Chapter 7: Trees

An Application: A Binary Search Tree

In-Class Work

Outline

1. Chapter 7: Trees
   - An Application: A Binary Search Tree
   - In-Class Work
Let’s recall **Binary Search Trees (BST):**
binary trees where every node has the following property:

- Each value in the left subtree is less than the value at the node.
- Each value in the right subtree is greater than the value at the node.  **No duplicates!**
Binary Search Trees in C++

In-Class Work

Binary Search With A Binary Tree

- Start at the root
- If the value is there, we are done
- If the value is less than the node value, search the left subtree
- If the value is greater than the node value, search the right subtree
Performance (Running Time) To Find A Value

- Average Performance is $\Theta(\log n)$. If the tree is not too unbalanced, then we divide the number of items to search in half at each node. This is actually a binary search.

- Worst-Case Performance is $\Theta(n)$. If the tree branches only to one side (left or right) this is the same as linear search.
TreeNode Class

Recursive Definition Of A TreeNode Class in Python

class TreeNode:
    def __init__(self, data = None, left=None, right=None):
        self.item = data
        self.left = left # TreeNode or None
        self.right = right # TreeNode or None
TreeNode Class

Recursive Definition of a TreeNode Class in C++

//TreeNode.h
class TreeNode{

public:
    TreeNode(int item, TreeNode *left = NULL, TreeNode*
    *right = NULL);

private:
    TreeNode(const TreeNode &tnode); // no Copy Constructor
    void operator=(const TreeNode &tnode); // no assignment

operator
    int _item;
    TreeNode* _left;
    TreeNode* _right;
}

See the files TreeNode.h, TreeNode.cpp, and usingTreeNode.cpp.
Implementing A BST

In Python: **\_\_init\_\_ (Constructor)**

```python
from TreeNode import TreeNode

class BST:
    def __init__(self):
        """ creates empty binary search tree ""

        self.root = None
```

 CSI33 Data Structures
Implementing A BST

IN C++ : BST.h

// BST.h
class BST{

public:
    BST() { _root = NULL; } // creates empty tree
    ~BST(); // destructor

private:
    TreeNode * _root;
};
Insertion into BST

For the following BST, let’s insert values 15, 34, and 79.
Insertion into BST

After insertion of 15, 34, and 79:
Insertion: Iterative or Recursive

Trees are a naturally recursive data structure, therefore it makes sense to implement insertion recursively, but we also have iterative version in Python’s implementation.

In C++ implementation, you can find an iterative implementation only, but check out the overloaded `cin` method...

See the file `BST.cpp`.
SEARCH: ITERATIVE OR RECURSIVE

Trees are a naturally recursive data structure, therefore it makes sense to implement search recursively as well. In Python’s implementation we had both (the recursive implementation was a HW assignment).

In C++ implementation, you can find an iterative implementation only.

See the file BST.cpp.
Deleting from a BST

Removing a specific item from a BST is a bit tricky. List of cases:

- the node to be removed is a leaf:
  then we can simply drop it off the tree
  (reference in its parent node is set to None)

- the node to be removed has a single child:
  then we can simply reset the reference from its parent to the
  reference to the node’s child instead.

- the node to be removed has two children:
  leave the node in place, but replace its contents (i.e. value), i.e.
  find an easily deletable node whose contents can be transferred into
  the target node, while maintaining the tree’s binary search property.
  (Two options there: rightmost node of the left subtree (our book),
  or leftmost node of the right subtree)
**Example 1**

Let's delete 5 from a BST:

![BST Diagram]

Before deletion:
- 10
  - 5
    - 3
    - 12
    - 17
  - 15

After deletion:
- 10
  - 3
    - 12
    - 17
  - 15
Example 2

Let’s delete 6 from a BST:

```
6
/  \
|   |
8   15
/  \
|    |
7    12
     /  \
    |    |
   8    17
```

```
10
/  \
|   |
8   15
/  \
|    |
7    12
     /  \
    |    |
   11   16
```
Example 3

Let’s delete 15 from the given BST:
Deletion from BST

Example 3

b) 

```
  10
 /   
5     15
|     /   
3  8   12
  |   /   |
  4 7  11 13
  |   |   |
  6   11 16
```
Example 3

Deletion from BST

b)
Example 3

An Application: A Binary Search Tree

Deletion from BST

Example 3

b)
Example 3
Example 3

Deletion from BST
Deletion from BST

Conclusion

In conclusion, we can say that when deleting a value from BTS, which is represented by a node with two children, our book follows the following procedure:

- step to the left sub-tree,
- locate the rightmost node (or a leaf) in it,
- and place its value in to the node with value to be deleted, making necessary adjustments of the references.

We implemented the deletion in Python, but don’t have its implementation in BST.cpp yet. This is a suggested practice.
Run-Time Analysis Of BST Methods

Methods

- `asList` is $\Theta(n)$.
- `insert`, `delete`, `find` have $\Theta(\log n)$ average behavior.
- `insert`, `delete`, `find` have $\Theta(n)$ worst-case behavior.
For the following, state whether each of them is a binary tree, a binary search tree (BST), or just a tree.
In-Class Work

In-Class Work - On Your Own, Part 2

Using class BST, insert the following numbers, one by one: 25, 5, 58, 1, 7, 17, 21, 32, 90, 6, 4, and 2.

1) Draw this BST as you think it should look.

2) What will be its array representation?

3) How will the tree look like if 5 is deleted?