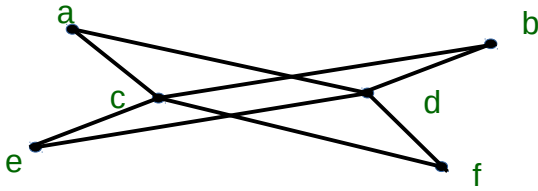
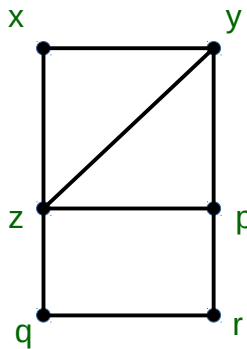
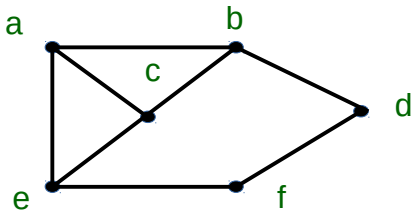


1. Consider the following graph:

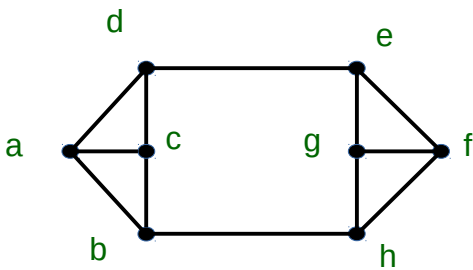


Is it possible to color the vertices with two colors, so that no two adjacent vertices have the same color?

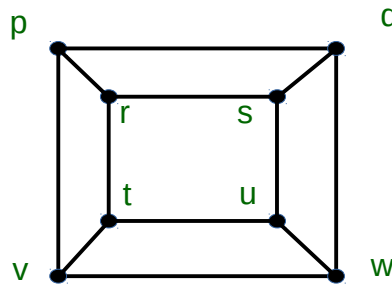
2. Determine whether the given pair of graphs is isomorphic:



3. Determine whether the given pair of graphs is isomorphic. If they are, give an isomorphism.



G



S

4. Two graphs, **G** and **H** are given by their matrix representations. Determine whether the graphs are isomorphic.

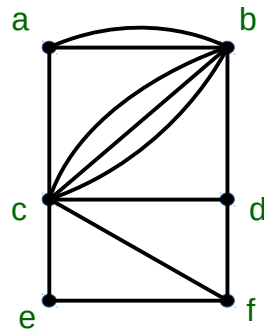
$$M_G = \begin{bmatrix} 1 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & 1 & 0 \end{bmatrix}$$

$$M_H = \begin{bmatrix} 1 & 1 & 0 \\ 1 & 0 & 1 \\ 0 & 1 & 1 \end{bmatrix}$$

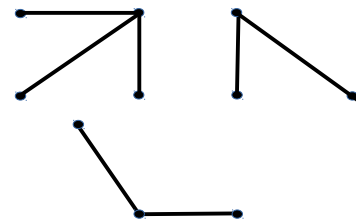
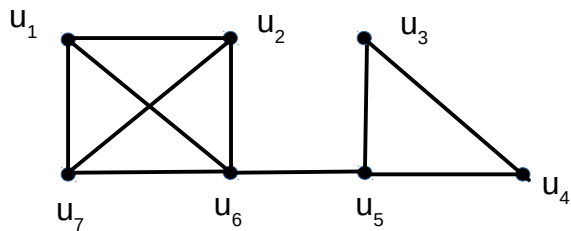
5. For the given undirected graph, give its:
 - adjacency list representation, and
 - matrix representation

to think about:

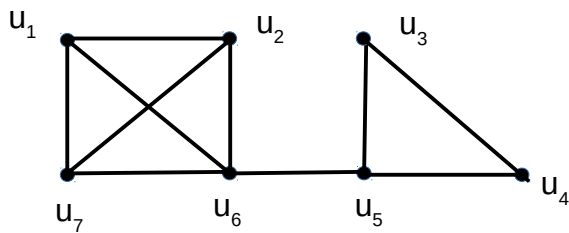
How to represent multiple edges?



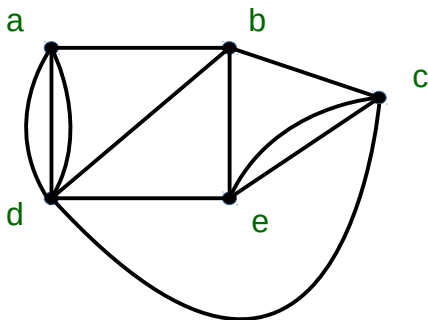
6. Determine whether the given undirected graphs are connected.



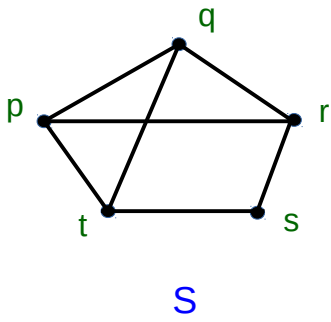
7. Determine whether the given undirected connected graph has a *cut vertex (articulation point)* and/or a *cut edge (bridge)*.



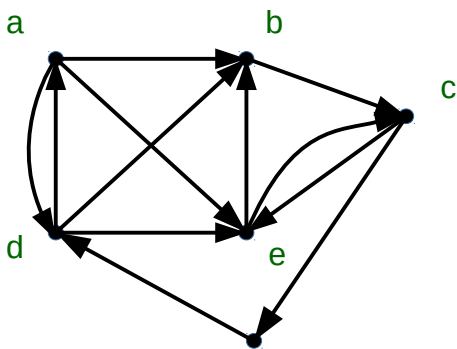
8. Determine whether the given connected undirected graph has Euler circuit? Euler trail?



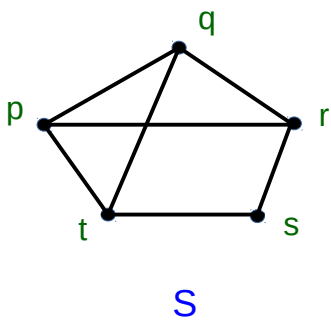
9. Determine whether the given connected undirected graph has Hamilton cycle? Hamilton path?



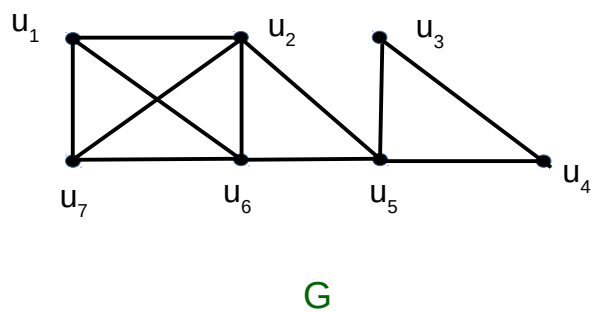
10. Determine whether the given connected directed graph has Hamilton cycle? Hamilton path?



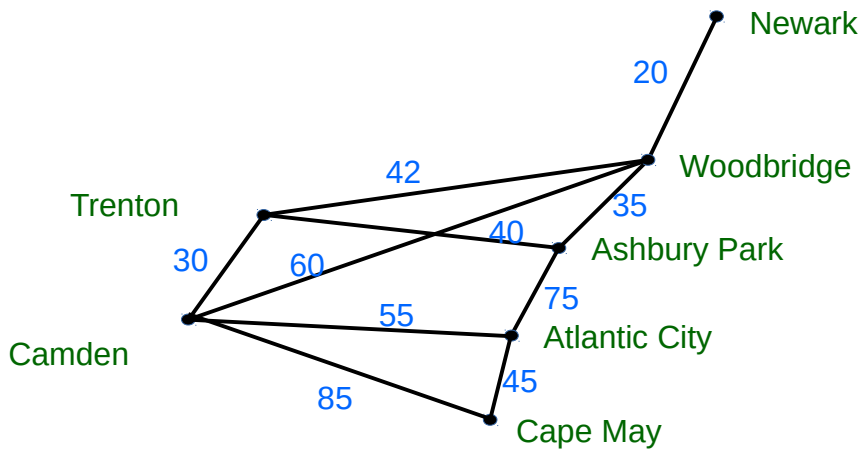
11. Determine if the graph is planar. If it is not, does it have a planar representation?



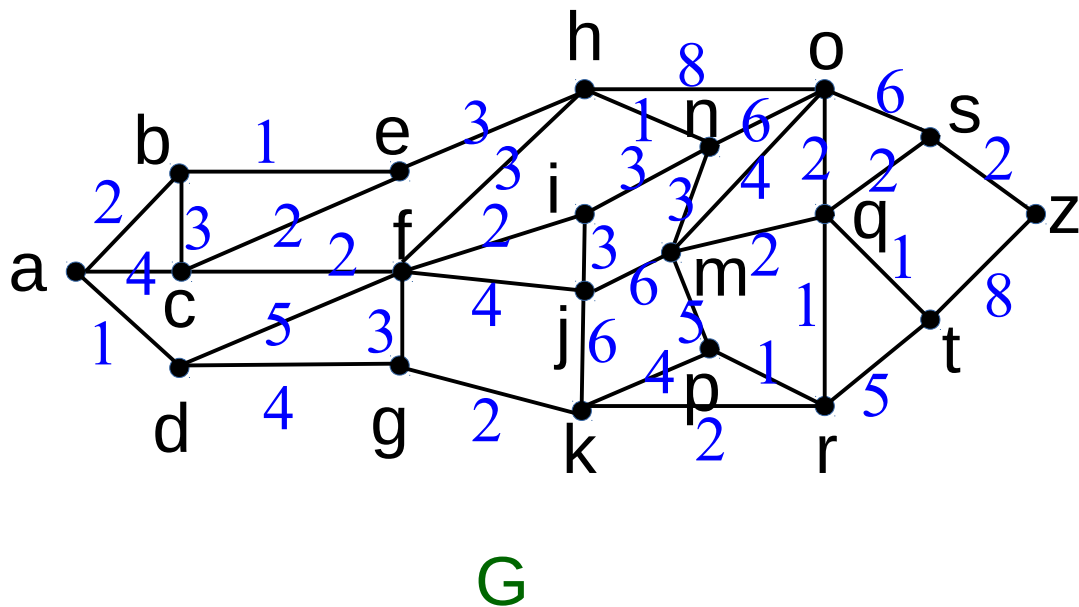
12. Find the chromatic number of the given graph G , $\chi(G)$.



13. Find the shortest (in miles) route from Camden city to Newark city.



14. Find the shortest path from **a** to **z** in the given graph **G**, using Dijkstra's algorithm for weighted graphs.



15. How many edges are in K_5 ? Is K_5 a regular graph?

16. Is it possible to have a 3-regular graph with five vertices? If such a graph is possible, draw an example. If such a graph is not possible, explain why not.

17. What is the longest possible walk in a graph with n vertices?

18. What is the longest possible cycle in a graph with n vertices?

19. Is K_6 planar?