

Vector components:  $A_x = A \cos \theta$ ,  $A_y = A \sin \theta$ ;

Vectors:

magnitude  $A = \sqrt{A_x^2 + A_y^2}$ ;  $\theta_{ref} = \tan^{-1} \frac{|A_y|}{|A_x|}$

Complex numbers:

$x + jy$  rectangular form;  $r \angle \theta = r(\cos \theta + j \sin \theta)$  polar form;  $re^{j\theta}$  exponential form

$$x = r \cos \theta, y = r \sin \theta; \quad r = \sqrt{x^2 + y^2}, \quad \theta_{ref} = \tan^{-1} \frac{y}{x}$$

$$x + jy = r(\cos \theta + j \sin \theta) = r \angle \theta$$

product:  $r_1 \angle \theta_1 \cdot r_2 \angle \theta_2 = (r_1 \cdot r_2) \angle (\theta_1 + \theta_2)$ ; quotient:  $\frac{r_1 \angle \theta_1}{r_2 \angle \theta_2} = \frac{r_1}{r_2} \angle (\theta_1 - \theta_2)$

DeMoivre's theorem:  $(r \angle \theta)^n = r^n \angle (n\theta)$

Logarithms and Exponential Functions:

$y = b^x$  exponential function, logarithmic form:  $\log_b y = x$

$y = \log_b x$  logarithmic function

$$\log_b xy = \log_b x + \log_b y \quad \log_b \frac{x}{y} = \log_b x - \log_b y \quad \log_b(x^n) = n \log_b x$$

$$\log_b 1 = 0 \quad \log_b b = 1 \quad \log_b(b^n) = n$$

$$\text{changing base of the logarithms: } \log_b x = \frac{\log_a x}{\log_a b} \quad \log_b x = \frac{\log x}{\log b} \quad \text{or} \quad \log_b x = \frac{\ln x}{\ln b}$$

Trigonometric functions and identities:

For graphs of  $y = a \sin(bx + c)$ ,  $y = a \cos(bx + c)$ ,  $y = a \csc(bx + c)$ , or  $y = a \sec(bx + c)$  :

the Amplitude =  $|a|$ , Period =  $\frac{2\pi}{b}$ , Displacement =  $-\frac{c}{b}$

5 'main' points (without displacement):  $0, \frac{Period}{4}, \frac{2 \cdot Period}{4}, \frac{3 \cdot Period}{4}, \frac{4 \cdot Period}{4}$

For the graphs of  $y = a \tan(bx + c)$  or  $y = a \cot(bx + c)$  : Period =  $\frac{\pi}{b}$

3 'main' points (without displacement):  $0, \frac{Period}{2}, \frac{2 \cdot Period}{2}$

$$\sin \theta \csc \theta = 1 \text{ or } \csc \theta = \frac{1}{\sin \theta} \quad (1) \quad \cos \theta \sec \theta = 1 \text{ or } \sec \theta = \frac{1}{\cos \theta} \quad (2) \quad \tan \theta = \frac{1}{\cot \theta} \quad (3)$$

$$\frac{\sin \theta}{\cos \theta} = \tan \theta \quad (4) \quad \frac{\cos \theta}{\sin \theta} = \cot \theta \quad (5) \quad \sin^2 \theta + \cos^2 \theta = 1 \quad (6)$$

$$1 + \tan^2 \theta = \sec^2 \theta \quad (7) \quad 1 + \cot^2 \theta = \csc^2 \theta \quad (8)$$

$$\sin(\alpha + \beta) = \sin \alpha \cos \beta + \sin \beta \cos \alpha \quad (9) \quad \sin(\alpha - \beta) = \sin \alpha \cos \beta - \sin \beta \cos \alpha \quad (10)$$

$$\cos(\alpha + \beta) = \cos \alpha \cos \beta - \sin \alpha \sin \beta \quad (11) \quad \cos(\alpha - \beta) = \cos \alpha \cos \beta + \sin \alpha \sin \beta \quad (12)$$

$$\tan(\alpha \pm \beta) = \frac{\tan \alpha \pm \tan \beta}{1 \mp \tan \alpha \tan \beta} \quad (13) \quad \tan(2\alpha) = \frac{2 \tan \alpha}{1 - \tan^2 \alpha} \quad (16)$$

$$\sin(2\alpha) = 2 \sin \alpha \cos \alpha \quad (14) \quad \cos(2\alpha) = \cos^2 \alpha - \sin^2 \alpha = 2 \cos^2 \alpha - 1 = 1 - 2 \sin^2 \alpha \quad (15)$$

$$\sin \frac{\theta}{2} = \pm \sqrt{\frac{1 - \cos \theta}{2}} \quad (17) \quad \cos \frac{\theta}{2} = \pm \sqrt{\frac{1 + \cos \theta}{2}} \quad (18)$$

$$-\frac{\pi}{2} \leq \sin^{-1} x \leq \frac{\pi}{2} \quad 0 \leq \cos^{-1} x \leq \pi \quad -\frac{\pi}{2} < \tan^{-1} x < \frac{\pi}{2} \quad 0 < \cot^{-1} x < \pi$$

$$0 \leq \sec^{-1} x \leq \pi \quad (\sec^{-1} x \neq \frac{\pi}{2}) \quad -\frac{\pi}{2} \leq \csc^{-1} x \leq \frac{\pi}{2} \quad (\csc^{-1} x \neq 0)$$

Solving systems of linear equations:

$$\begin{vmatrix} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ a_3 & b_3 & c_3 \end{vmatrix}$$